

This is a try for the solution of Laplace Equation.

The uncompleted solution is

$$\phi = \sum_{m=0}^{\infty} A_m \sinh\left(\frac{P_m}{a} z\right) BesselJ\left(0, \frac{P_m}{a} r\right)$$

Where  $BesselJ(0, P_m) = 0$ , that is  $P_m$ , ( $m = 1, 2, 3 \dots$ ) is the solution of  $BesselJ(0, x) = 0$ , and

$z$  is the  $z$  axis of cylinder coordinate and  $r$  is the  $r$  axis. In the case, the distribution of potential  $\phi$  has no relationship with  $\theta$  of cylinder coordinate.

Using the given boundary condition  $\phi(r, h) = U_0$ , we can get

$$U_0 = \sum_{m=0}^{\infty} A_m \sinh\left(\frac{P_m}{a} h\right) BesselJ\left(0, \frac{P_m}{a} r\right) \quad (1)$$

Now need to solve the formula of  $A_m$ .

The method on the book is that:

Multiply  $r \times BesselJ\left(0, \frac{P_m}{a} r\right)$  on both sides of the equal mark, then integral and because of the orthogonality of Bessel function, we have

$$A_m = \frac{\int_0^a U_0 \times r \times BesselJ\left(0, \frac{P_m}{a} r\right) dr}{\int_0^a r \times \sinh\left(\frac{P_m}{a} h\right) \times [BesselJ\left(0, \frac{P_m}{a} r\right)]^2 dr} \quad (2)$$

I really do not know what the basis of above equation is. Why can we get (2) from (1)? Does anyone give me any advice?

Thanks in advance.

Regards

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