

Using the Spreadsheet Complex Matrix by Decomposition

In the screen shot below we are using the spreadsheet to solve the three complex simultaneous equation:

$$\mathbf{Z}_{1A}\mathbf{I}_1 + \mathbf{Z}_{1B}\mathbf{I}_2 + \mathbf{Z}_{1C}\mathbf{I}_3 = \mathbf{V}_1$$

$$\mathbf{Z}_{2A}\mathbf{I}_1 + \mathbf{Z}_{2B}\mathbf{I}_2 + \mathbf{Z}_{2C}\mathbf{I}_3 = \mathbf{V}_2$$

$$\mathbf{Z}_{3A}\mathbf{I}_1 + \mathbf{Z}_{3B}\mathbf{I}_2 + \mathbf{Z}_{3C}\mathbf{I}_3 = \mathbf{V}_3$$

where $\mathbf{V}_1 = 6 + j5$ volts, $\mathbf{V}_2 = 20 + j0$ volts and $\mathbf{V}_3 = 20 + j20$ volts

$$\mathbf{Z}_{1A} = 7 + j9 \Omega, \mathbf{Z}_{1B} = 5 + j1 \Omega, \mathbf{Z}_{1C} = 0 + j1 \Omega,$$

$$\mathbf{Z}_{2A} = 1 + j9 \Omega, \mathbf{Z}_{2B} = 0 + j0 \Omega, \mathbf{Z}_{2C} = -5 + j-5 \Omega,$$

$$\mathbf{Z}_{3A} = 1 + j1 \Omega, \mathbf{Z}_{3B} = 5 + j7 \Omega, \mathbf{Z}_{3C} = 0 + j0 \Omega$$

$[R]$ <table border="1" style="border-collapse: collapse; width: 100%;"> <tr><td>7.000</td><td>5.000</td><td>0.000</td></tr> <tr><td>1.000</td><td>0.000</td><td>-5.000</td></tr> <tr><td>1.000</td><td>5.000</td><td>0.000</td></tr> </table> $Det[R] = 150$	7.000	5.000	0.000	1.000	0.000	-5.000	1.000	5.000	0.000	$[X]$ <table border="1" style="border-collapse: collapse; width: 100%;"> <tr><td>9.00</td><td>1.00</td><td>1.00</td></tr> <tr><td>9.00</td><td>0.00</td><td>-5.00</td></tr> <tr><td>1.00</td><td>7.00</td><td>0.00</td></tr> </table> $Det[X] = 373$	9.00	1.00	1.00	9.00	0.00	-5.00	1.00	7.00	0.00	x <table border="1" style="border-collapse: collapse; width: 100%;"> <tr><td>1.36E-01</td><td></td></tr> <tr><td>3.20E+00</td><td></td></tr> <tr><td>-2.62E+00</td><td></td></tr> </table> $+j$ <table border="1" style="border-collapse: collapse; width: 100%;"> <tr><td>9.51E-01</td><td></td></tr> <tr><td>-6.91E-01</td><td></td></tr> <tr><td>3.06E+00</td><td></td></tr> </table>	1.36E-01		3.20E+00		-2.62E+00		9.51E-01		-6.91E-01		3.06E+00		$=$ <table border="1" style="border-collapse: collapse; width: 100%;"> <tr><td>6.000</td><td></td></tr> <tr><td>20.000</td><td></td></tr> <tr><td>20.000</td><td></td></tr> </table> $[V]$ <table border="1" style="border-collapse: collapse; width: 100%;"> <tr><td>5.000</td><td></td></tr> <tr><td>0.000</td><td></td></tr> <tr><td>20.000</td><td></td></tr> </table>	6.000		20.000		20.000		5.000		0.000		20.000	
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The solution is:

$$\mathbf{I}_1 = 0.136 + j0.951 \text{ A}$$

$$\mathbf{I}_2 = 3.2 - j0.691 \text{ A}$$

$$\mathbf{I}_3 = -2.62 + j3.06 \text{ A.}$$

