

$$\begin{aligned}
 E &= kq \left[ \frac{1}{x^2} - \frac{x}{(R^2 + x^2)^{\frac{3}{2}}} \right] = kq \left\{ \frac{1}{x^2} - \frac{x}{x^3 \left[ 1 + \left( \frac{R}{x} \right)^2 \right]^{\frac{3}{2}}} \right\} \approx kq \left\{ \frac{1}{x^2} - \frac{1}{x^2 \left[ 1 + \frac{3}{2} \left( \frac{R}{x} \right)^2 + \dots \right]} \right\} = \\
 &= kq \frac{1 + \frac{3}{2} \left( \frac{R}{x} \right)^2 - 1}{x^2 \left( 1 + \frac{3}{2} \frac{R^2}{x^2} \right)} \approx kq \frac{\frac{3}{2} \frac{R^2}{x^2}}{x^2 + \frac{3}{2} R^2} = kq \frac{3}{2} \frac{R^2}{x^4} = \frac{3qR^2}{8\pi\epsilon_0 x^4}
 \end{aligned}$$

Explanations:

$$\left[ 1 + \left( \frac{R}{x} \right)^2 \right]^{\frac{3}{2}} = 1 + \frac{3}{2} \left( \frac{R}{x} \right)^2 + \dots \approx 1 + \frac{3}{2} \left( \frac{R}{x} \right)^2 \dots \text{series expansion}$$

$$x^2 + \frac{3}{2} R^2 \approx x^2 \dots \text{because } x \gg R$$