



$$I_1 = \int_{R-r}^{R-\frac{r^2}{2R}} dx \int_0^{\sqrt{r^2-(x-R)^2}} dy = \int_{R-r}^{R-\frac{r^2}{2R}} \sqrt{r^2-(x-R)^2} dx$$

$$I_2 = \int_{R-\frac{r^2}{2R}}^R dx \int_0^{\sqrt{R^2-x^2}} dy = \int_{R-\frac{r^2}{2R}}^R \sqrt{R^2-x^2} dx$$