



$$mg = N \cos x + F \sin x$$

$$\frac{mv^2}{r} = N \sin x - F \cos x$$

$$(mg)^2 = N^2 \cos^2 x + F^2 \sin^2 x + 2NF \cos x \sin x$$

$$\left(\frac{mv^2}{r}\right)^2 = N^2 \sin^2 x + F^2 \cos^2 x - 2NF \cos x \sin x$$

$$(mg)^2 + \left(\frac{mv^2}{r}\right)^2 = N^2 + F^2$$

$$mg \sin x = N \sin x \cos x + F \sin^2 x$$

$$mg \cos x = N \cos^2 x + F \sin x \cos x$$

$$\frac{mv^2}{r} \sin x = N \sin^2 x - F \sin x \cos x$$

$$\frac{mv^2}{r} \cos x = N \sin x \cos x - F \cos^2 x$$

$$mg \sin x - \frac{mv^2}{r} \cos x = F$$

$$mg \cos x + \frac{mv^2}{r} \sin x = N$$

With $\frac{mv^2}{r}$ taken as a **centrifugal** force, there is no acceleration.

$$N = mg \cos x + \frac{mv^2}{r} \sin x$$

$$F = mg \sin x - \frac{mv^2}{r} \cos x$$

$$N^2 = (mg)^2 \cos^2 x + \left(\frac{mv^2}{r}\right)^2 \sin^2 x + 2mg \left(\frac{mv^2}{r}\right) \sin x \cos x$$

$$F^2 = (mg)^2 \sin^2 x + \left(\frac{mv^2}{r}\right)^2 \cos^2 x - 2mg \left(\frac{mv^2}{r}\right) \sin x \cos x$$

$$N^2 + F^2 = (mg)^2 + \left(\frac{mv^2}{r}\right)^2$$