

## Thevenin's theorem -

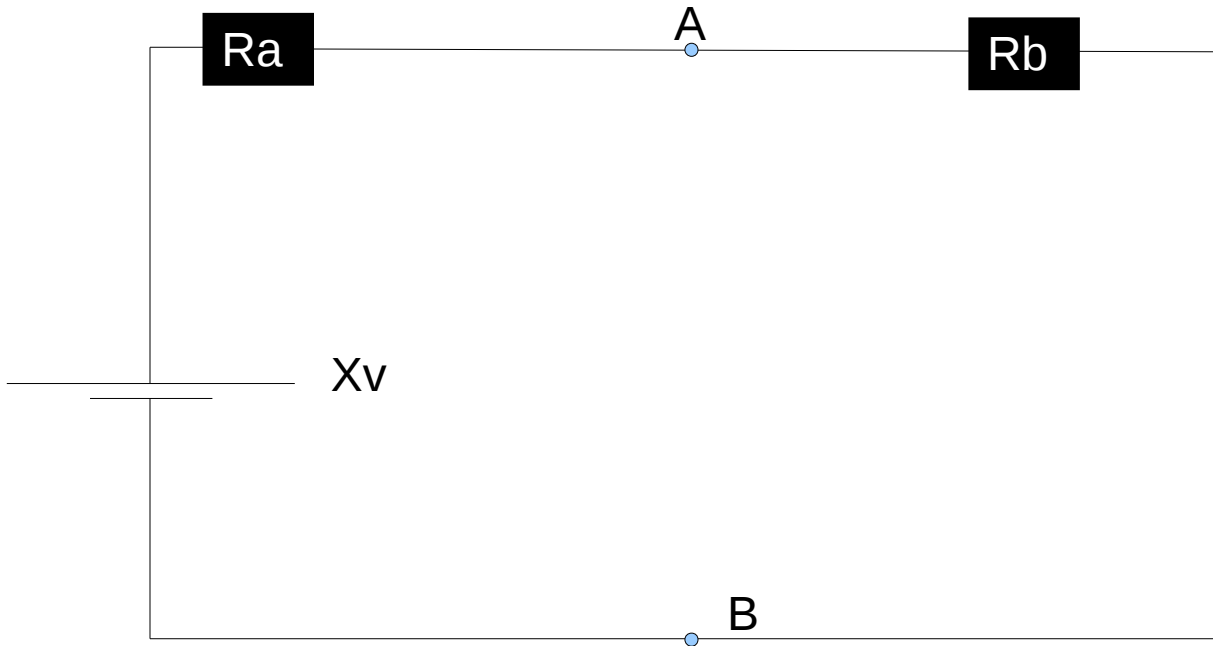


Fig. a

Deriving potential difference between points A and B -

$$\text{Total } I = \frac{V}{R} = \frac{X_v}{R_a + R_b}$$

$$V \text{ across } R_a = I_{\text{total}} R_a$$

Potent across  $R_b$  = potential across A and B.

$$\text{Potential across } R_b = X_v - I_{\text{total}} R_a$$

$$= X_v - \frac{X_v}{R_a + R_b} R_a$$

$$X_v \left( 1 - \frac{1}{R_a + R_b} R_a \right)$$

$$\text{Resistance between A and B} - \frac{R_a R_b}{R_a + R_b}$$

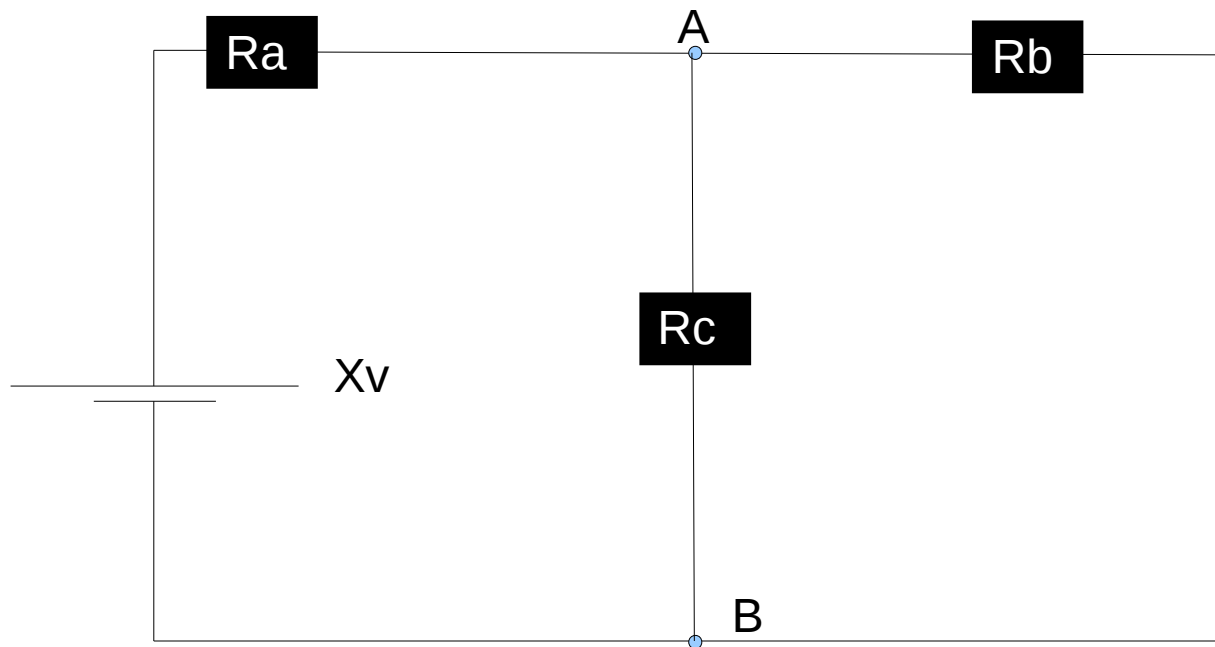


Fig. b

On adding the resistance  $R_c$  (as in the above image) -

$$\text{Total } I = \frac{X_v}{\frac{R_c.R_b}{R_c + R_b} + R_a}$$

$$V \text{ across } R_b \text{ or } R_c = I_{\text{total}} \frac{R_c.R_b}{R_c + R_b} \quad \text{or} \quad \frac{X_v}{\frac{R_c.R_b}{R_c + R_b} + R_a} \frac{R_c.R_b}{R_c + R_b}$$

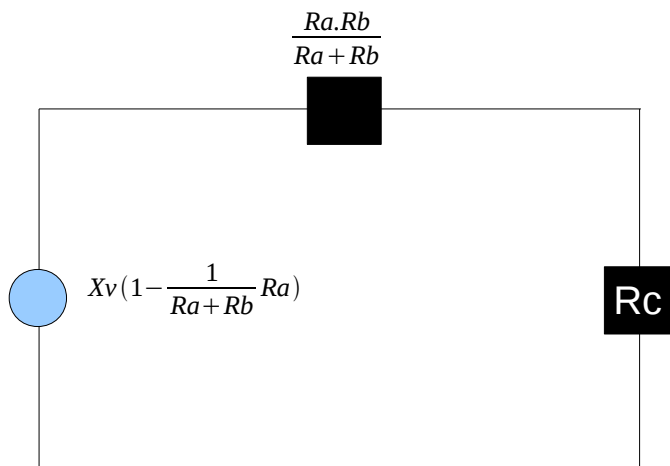
$$\frac{X_v.R_c.R_b}{\left(\frac{R_c.R_b}{R_c + R_b} + R_a\right)(R_c + R_b)}$$

$$\frac{X_v.R_c.R_b}{\left(\frac{R_c.R_b + (R_c + R_b)R_a}{R_c + R_b}\right)(R_c + R_b)}$$

$$\frac{X_v.R_c.R_b}{(R_c.R_b + R_a.R_c + R_b.R_a)}$$

Connect this resistance in series to a voltage source equal to the rating of the potential difference between the 2 open points (as computed before, between A and B), and then, again in series, add Rc...or the load resistance.

The P.D that should come across Rc should be equal to as figured out in the derivations of figure B (  $\frac{Xv.Rc.Rb}{(Rc.Rb+Ra.Rc+Rb.Ra)}$  )



As you would have assumed, that blue thing is the voltage source.

$$\text{Total resistance} = \frac{Ra.Rb}{Ra + Rb} + Rc$$

The total current in this case will be -

$$i = \frac{Xv(1 - \frac{1}{Ra + Rb} Ra)}{\frac{Ra.Rb}{Ra + Rb} + Rc}$$

$$\text{So } V_{Rc} = \left( \frac{Xv(1 - \frac{1}{Ra + Rb} Ra)}{\frac{Ra.Rb}{Ra + Rb} + Rc} \right) \left( \frac{Ra.Rb}{Ra + Rb} + Rc \right)$$

$$V_{Rc} = Xv(1 - \frac{1}{Ra + Rb} Ra)$$

Which does not appear to be equal to  $\frac{Xv.Rc.Rb}{(Rc.Rb+Ra.Rc+Rb.Ra)}$