

Well the main question here is why the next happens:

$$\frac{1}{mw} \frac{d^2\psi}{dx^2} = \frac{d^2\psi}{d\xi^2} \quad (1)$$

Because if you take the second derivative of ξ you get this:

$$\frac{d\xi}{dx} = \sqrt{\frac{m\omega}{\hbar}} \Rightarrow \frac{d^2\xi}{dx^2} = 0 \quad (2)$$

Because:

$$\sqrt{\frac{m\omega}{\hbar}} = \text{constant} \quad (3)$$