

$i = \dot{Q}$   
 $i = C \dot{V}$   
 $I = 5C V$

Initial voltage equal to zero in the capacitor

$$\begin{cases} R_1 I_1 + R_{12}(I_1 - I_2) + \frac{1}{5C}(I_1 - I_2) = 12 \\ R_{12}(I_2 - I_1) + \frac{1}{5C}(I_2 - I_1) + R_2 I_2 = 0 \end{cases}$$

$$\begin{cases} R_1 I_1 + (R_{12} + \frac{1}{5C})(I_1 - I_2) = 12 \\ -(R_{12} + \frac{1}{5C})(I_1 - I_2) + R_2 I_2 = 0 \end{cases}$$

$$\begin{aligned} (R_1 + R_{12} + \frac{1}{5C}) I_1 - (R_{12} + \frac{1}{5C}) I_2 &= 12 \\ -(R_{12} + \frac{1}{5C}) I_1 + (R_2 + R_{12} + \frac{1}{5C}) I_2 &= 0 \end{aligned}$$

$$\begin{bmatrix} R_1 + R_{12} + \frac{1}{5C} & -(R_{12} + \frac{1}{5C}) \\ -(R_{12} + \frac{1}{5C}) & R_2 + R_{12} + \frac{1}{5C} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 12 \\ 0 \end{bmatrix}$$

Wolfram's solution (I left it to C, because it's small and inconvenient):

$$I_1(s) = \frac{96C s + 12}{32C s + 7} \rightsquigarrow i_1(t) = \frac{-300 e^{-7t/32C}}{96C}, \quad t > 0$$

$$I_2(s) = \frac{36C s + 12}{32C s + 7} \rightsquigarrow i_2 = \frac{120 e^{-7t/32C}}{96C}, \quad t > 0$$

Problems with this solution (differ from the method using resolving EDO directly):

- If I put to include  $t = 0$ , a Dirac delta appears in the currents
- For  $t \rightarrow \infty$ , I expected the two currents to be equal
- For infinite  $t$  the two currents can be zero.
- And it also happened that the current  $i_1$  is negative, but it must be positive;